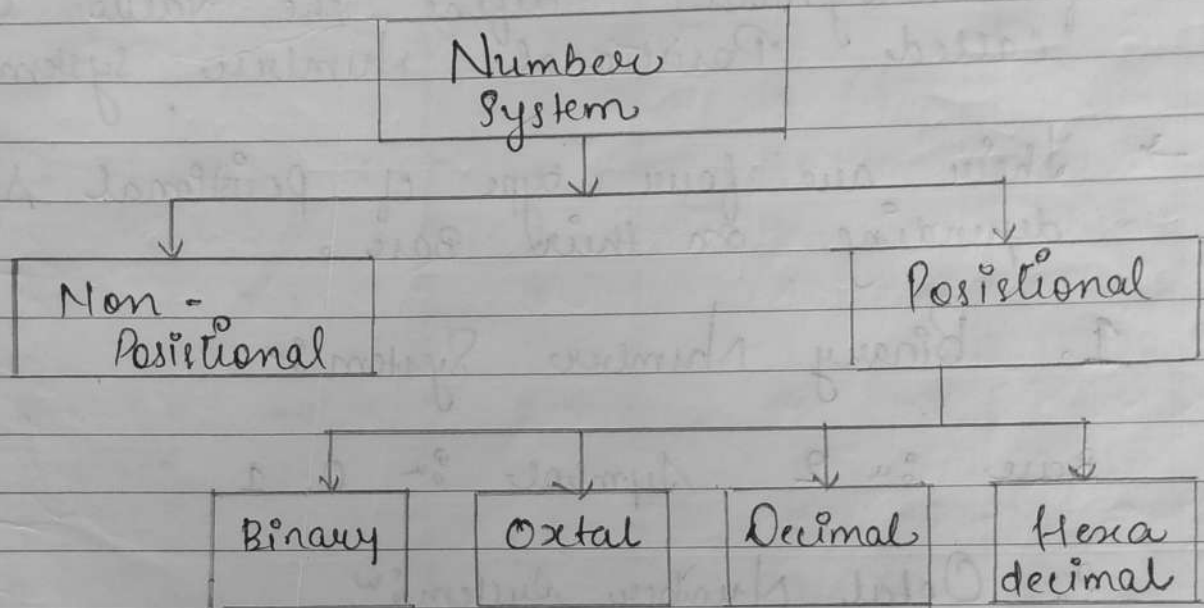


318116

Unit 3 :-Number System :-* Non Positional Number System :-

→ In this number system each symbol represent the same value, regardless of its position in the number.

→ Advantage :-

- It is very difficult to perform Arithmetic operation with non positional Number system.

* Positional Number System :-

- The number system, in which position of the symbol define the value is called Positional Number System.
- There are four type of positional system depending on their Base.

1. Binary Number System :-

Base :- 2 Symbol :- 0, 1

2. Octal Number System :-

Base :- 8 Symbol :- 0, 1, 2, 3, 4, 5, 6, 7

3. Decimal Number System :-

Base :- 10 Symbol :- 0, 1, 2, 3, 4, 5, 6, 7, 8, 9

4. Hexadecimal Number System :-

Base :- 16 Symbol :- 0, 1, 2, 3, 4, 5, 6, 7, 8, 9, A, B, C, D, E, F

$$1^0 = 1, 2^0 = 1, 3^0 = 1, n^0 = 1$$

* Relationship between Decimal, Octal, Hexa-Decimal and Binary :-

| Digit | Decimal | Octal | Hexadecimal | Binary |
|-------|---------|-------|-------------|--------|
| 0 | 0 | 0 | 0 | 0000 |
| 1 | 1 | 1 | 1 | 0001 |
| 2 | 2 | 2 | 2 | 0010 |
| 3 | 3 | 3 | 3 | 0011 |
| 4 | 4 | 4 | 4 | 0100 |
| 5 | 5 | 5 | 5 | 0101 |
| 6 | 6 | 6 | 6 | 0110 |
| 7 | 7 | 7 | 7 | 0111 |
| 8 | 8 | | 8 | 1000 |
| 9 | 9 | | 9 | 1001 |
| 10 | | | A | 1010 |
| 11 | | | B | 1011 |
| 12 | | | C | 1100 |
| 13 | | | D | 1101 |
| 14 | | | E | 1110 |
| 15 | | | F | 1111 |

10 A

0
20 = 0000
0010

$$2 \sqrt{1}$$

$$2 \overline{) \begin{array}{r} 1 \\ 0 \end{array} }$$

* Types Of Conversion

1. Binary to Decimal

2. Octal to Decimal

3. Hexa to Decimal

4. Decimal to Binary

5. Decimal to Octal

6. Decimal to Hexa

7. Binary to Octal

8. Binary to Hexa

9. Octal to Binary

10. Hexa to Binary

11. Octal to Hexa

12. Hexa to Octal

Others to Decimal
Method : Multiplication

Decimal to Others
Method : Division

Method : Divided into
group of three

Method : Divided into
group of four

Method : Divide into
group of three

Method : Divided into
group of four

1. Binary to Decimal

$$1. (100111)_2 = (?)_{10}$$

⇒

$$(1 \times 2^0) + (1 \times 2^1) + (1 \times 2^2) + (0 \times 2^3) + (0 \times 2^4) + (1 \times 2^5)$$

$$= (1 \times 1) + (1 \times 2) + (1 \times 4) + (0 \times 8) + (0 \times 16) + (1 \times 32)$$

$$= 1 + 2 + 4 + 32$$

$$= 39$$

$$2. \overbrace{(11010011)}_76543210_2 = (?),_{10}$$

$$\begin{aligned}
 &= (1 \times 2^0) + (1 \times 2^1) + (0 \times 2^2) + (0 \times 2^3) + \\
 &\quad (1 \times 2^4) + (0 \times 2^5) + (1 \times 2^6) + (1 \times 2^7) \\
 &= (1 \times 1) + (1 \times 2) + (0 \times 4) + (0 \times 8) + \\
 &\quad (1 \times 16) + (0 \times 32) + (1 \times 64) + (1 \times 128) \\
 &= 1 + 2 + 16 + 64 + 128 \\
 &= 211
 \end{aligned}$$

Ans: $(11010011)_2 = (211)_{10}$

$$3. \overbrace{(11101011)}_76543210_2 = (?),_{10}$$

$$\begin{aligned}
 &= (1 \times 2^0) + (1 \times 2^1) + (0 \times 2^2) + (1 \times 2^3) + (0 \times 2^4) + \\
 &\quad (1 \times 2^5) + (1 \times 2^6) + (1 \times 2^7) \\
 &= (1 \times 1) + (1 \times 2) + (0 \times 4) + (1 \times 8) + (0 \times 16) + \\
 &\quad (1 \times 32) + (1 \times 64) + (1 \times 128) \\
 &= 1 + 2 + 8 + 32 + 64 + 128 \\
 &= 235
 \end{aligned}$$

Ans: $(11101011)_2 = (235)_{10}$

4. Binary to Decimal
Fractional No:

$$\overbrace{(101100.011)}_543210 \cdot 10^{-3}_2 = (?),_{10}$$

$$101100$$

$$\begin{aligned}
 &= (0 \times 2^0) + (0 \times 2^1) + (1 \times 2^2) + (1 \times 2^3) + (0 \times 2^4) + (1 \times 2^5) \\
 &= (0 \times 1) + (0 \times 2) + (1 \times 4) + (1 \times 8) + (0 \times 16) + (1 \times 32)
 \end{aligned}$$

$$= 4 + 8 + 32$$

$$= 44$$

$$\rightarrow 011$$

$$= (0 \times 2^{-1}) + (1 \times 2^{-2}) + (1 \times 2^{-3})$$

$$= (0 \times 1/2) + (1 \times 1/4) + (1 \times 1/8)$$

$$= \frac{1}{4} + \frac{1}{8}$$

$$= \frac{3}{8}$$

$$= 0.375$$

$$\text{Ans. } (101100.011) = (44.375)$$

$$5. (110110.0111)_2 = (?),_{10}$$

$$\begin{array}{r} 110110 \\ = (0 \times 2^0) + (1 \times 2^1) + (1 \times 2^2) + (0 \times 2^3) + (1 \times 2^4) + (1 \times 2^5) \end{array}$$

$$= (0 \times 2^{-1}) + (1 \times 2^{-2}) + (1 \times 2^{-3}) + (1 \times 2^{-4})$$

$$= (0 \times 1) + (1 \times 2) + (1 \times 4) + (0 \times 8) + (1 \times 16) + (1 \times 32)$$

$$= 2 + 4 + 16 + 32$$

$$= 54$$

$$= (0 \times 1/2) + (1 \times 1/4) + (1 \times 1/8) + (1 \times 1/16)$$

$$= \frac{1}{4} + \frac{1}{8} + \frac{1}{16}$$

$$= \frac{4 + 2 + 1}{16} = \frac{7}{16} = 0.4375$$

Ans. (101100.011)

Ans $(110110.0111)_2 = (54.4375)_{10}$

2. Octal to Decimal :-

1. $(2614)_8 = (?)_{10}$

$$\begin{aligned}
 &= (4 \times 8^0) + (1 \times 8^1) + (6 \times 8^2) + (2 \times 8^3) \\
 &= (4 \times 1) + (1 \times 8) + (6 \times 64) + (2 \times 512) \\
 &= 4 + 8 + 384 + 1024 \\
 &= 1420
 \end{aligned}$$

Ans: $(2614)_8 = (1420)_{10}$

2. $(562)_8 = (?)_{10}$

$$\begin{aligned}
 &= (2 \times 8^0) + (6 \times 8^1) + (5 \times 8^2) \\
 &= (2 \times 1) + (6 \times 8) + (5 \times 64) \\
 &= 2 + 48 + 320 \\
 &= 370
 \end{aligned}$$

Ans : $(562)_8 = (370)_{10}$

fractional No.:

$$3. (257.65)_8 = (?)_{10}$$

$$257$$

$$= (7 \times 8^0) + (5 \times 8^1) + (2 \times 8^2)$$

$$= 7 + 40 + 128 = 175$$

$$0.65$$

$$= (6 \times 8^{-1}) + (5 \times 8^{-2})$$

$$= (6 \times 1/8) + (5 \times 1/64)$$

$$= 6/8 + 5/64$$

$$= 48 + 5$$

$$64$$

$$= \frac{53}{64}$$

$$64$$

$$= 0.828$$

$$\text{Ans: } (257.65)_8 = (175.828)_{10}$$

or

3. Hexa to Decimal :

$$1. (2A3B)_{16} = (?)_{10}$$

$$\begin{aligned}
 &= (B \times 16^0) + (3 \times 16^1) + (A \times 16^2) + (2 \times 16^3) \\
 &= (11 \times 1) + (3 \times 16) + (10 \times 256) + (2 \times 4096) \\
 &= 11 + 48 + 2560 + 8192 \\
 &= 10811
 \end{aligned}$$

$$\text{Ans: } (2A3B)_{16} = (10811)_{10}$$

$$2. (FDE)_{16} = (?)_{10}$$

$$\begin{aligned}
 &= (E \times 16^0) + (D \times 16^1) + (F \times 16^2) \\
 &= (14 \times 1) + (13 \times 16) + (15 \times 256) \\
 &= 14 + 208 + 3840 \\
 &= 4062
 \end{aligned}$$

$$\text{Ans: } (FDE)_{16} = (4062)_{10}$$

\Rightarrow Fractional :

$$3. (A4E.D4)_{16} = (?)_{10}$$

$$\begin{array}{r}
 A4E \\
 210
 \end{array}$$

$$\begin{aligned}
 &= (A \times 16^2) + (4 \times 16^1) + (E \times 16^0) \\
 &= (14 \times 1) + (4 \times 16) + (10 \times 256) \\
 &= 14 + 64 + 2560 \\
 &= 2638
 \end{aligned}$$

D4
→
1-2

$$= (13 \times 16^{-1}) + (4 \times 16^{-2})$$

$$= (13 \times 1/16) + (4 \times 1/256)$$

$$= \frac{13}{16} + \frac{4}{256}$$

$$= \frac{208 + 4}{256}$$

$$= \frac{212}{256}$$

$$= 0.828$$

$$\text{Ans: } (A4E.D4)_{16} = (2638.828)_{10}$$

$$4. (2B.C4)_{16} = (?)_{10}$$

$$2B$$

$$= (2 \times 16^1) + (11 \times 16^0)$$

$$= (32 + 11)$$

$$= 43$$

$$= 43$$

C4

$$= (12 \times 16^{-1}) + (4 \times 16^{-2})$$

$$= (12 \times 1/16) + (4 \times 1/256)$$

$$= \frac{12}{16} + \frac{4}{256}$$

$$= \frac{192 + 4}{256}$$

$$= 0.765$$

$$(2B.C4)_{16} = (43.765)_{10}$$

4. Decimal to Binary

1. $(952)_{10} = (?)_2$

| | | |
|---|-----|---|
| 2 | 952 | 0 |
| 2 | 476 | 0 |
| 2 | 238 | 0 |
| 2 | 119 | 1 |
| 2 | 59 | 1 |
| 2 | 29 | 1 |
| 2 | 14 | 0 |
| 2 | 7 | 1 |
| 2 | 3 | 1 |
| 1 | | |

$(952)_{10} = (1110111000)_2$

2. $(428)_{10} = (?)_2$

| | | |
|---|-----|---|
| 2 | 428 | 0 |
| 2 | 214 | 0 |
| 2 | 107 | 1 |
| 2 | 53 | 1 |
| 2 | 26 | 0 |
| 2 | 13 | 1 |
| 2 | 6 | 0 |
| 2 | 3 | 1 |
| 1 | | |

$(428)_{10} = (110101100)_2$

→ Fractional No.:

1. $(247.65)_{10} = (?)_2$

$$\begin{array}{r} 2 \ 247 \ 1 \\ 2 \ 123 \ 1 \\ 2 \ 61 \ 1 \\ 2 \ 30 \ 0 \\ 2 \ 15 \ 1 \\ 2 \ 7 \ 1 \\ 2 \ 3 \ 1 \\ 1 \end{array}$$

$$0.65 \times 2 = 1.30 = 1$$

$$0.30 \times 2 = 0.60 = 0$$

$$0.60 \times 2 = 1.20 = 1$$

$$0.20 \times 2 = 0.40 = 0$$

$$0.40 \times 2 = 0.80 = 0$$

Ans:

$$(247.65)_{10} = (11110111.10100)_2$$

2. $(125.46)_{10} = (?)_2$

$$\begin{array}{r} 2 \ 125 \ 1 \\ 2 \ 62 \ 0 \\ 2 \ 31 \ 1 \\ 2 \ 15 \ 1 \\ 2 \ 7 \ 1 \\ 2 \ 3 \ 1 \\ 1 \end{array}$$

$$0.46 \times 2 = 0.92 = 0$$

$$0.92 \times 2 = 1.84 = 1$$

$$0.84 \times 2 = 1.68 = 1$$

$$0.68 \times 2 = 1.36 = 1$$

$$0.36 \times 2 = 0.72 = 0$$

Ans:

$$(125.46)_{10} = (1111101.01110)_2$$

6. Decimal to Hexa :

1. $(435)_{10} = (?)_{16}$

| | | |
|----|-----|----|
| 16 | 435 | 3 |
| 16 | 27 | 11 |
| | 1 | |

$(435)_{10} = (1B3)_{16}$

 \Rightarrow Fractional No :

$(931.62)_{10} = (?)_{16}$

| | | |
|----|-----|----|
| 16 | 931 | 3 |
| 16 | 58 | 10 |
| | 3 | |

$0.62 \times 16 = 9.92 = 9$

$0.92 \times 16 = 14.72 = 14 \text{ DE}$

$0.72 \times 16 = 11.52 = 11 \text{ B}$

$0.52 \times 16 = 8.32 = 8$

$0.32 \times 16 = 5.12 = 5$

Ans: $(931.62)_{10} = (3A3.9EB85)_{16}$

$(3233.56)_{10} = (?)_{16}$

| | | |
|----|------|----|
| 16 | 3233 | 1 |
| 16 | 202 | 10 |
| | 12 | |

$0.56 \times 16 = 9$

$(CA1.8F5C)_{16}$

$$\begin{array}{r}
 16 \\
 3 \\
 \hline
 48 \\
 3 \\
 \hline
 0.56 \\
 \times 16 \\
 \hline
 560 \\
 336 \\
 \hline
 96
 \end{array}$$

7. Binary to Octal :-

(421 Method)

$\begin{matrix} 2 & 1 & 0 \\ 2 & 2 & 2 \\ 4 & 2 & 1 \end{matrix}$

$$1. (1010101100)_2 = (?)_8$$

$$\begin{array}{ccccccc} 1 & 0 & 1 & 0 & 1 & 0 & 1 & 1 & 0 & 0 \\ \hline & 1 & & 2 & & 5 & & 4 & & \end{array}$$

$$(1010101100)_2 = (1254)_8$$

$$2. (10110011001)_2 = (?)_8$$

$$\begin{array}{ccccccc} 1 & 0 & 1 & 1 & 0 & 0 & 1 & 1 & 0 & 0 & 1 \\ \hline & 2 & & 6 & & 3 & & 1 & & \end{array}$$

$$\text{Ans :- } (10110011001)_2 = (2631)_8$$

$$(1101011)$$

$$(11010)$$

$$(10110011)$$

$$(11011101)$$

$$3. (1101011)_2 = (?)_8$$

$$\begin{array}{ccccccc} 1 & 1 & 0 & 1 & 0 & 1 & 1 \\ \hline & 1 & & 5 & & 3 & \end{array}$$

$$\text{Ans :- } (1101011)_2 = (153)_8$$

$$4. (11010)_2 = (?)_8$$

$$\begin{array}{ccccccc} 1 & 1 & 0 & 1 & 0 \\ \hline & 3 & & 2 & \end{array}$$

$$\text{Ans :- } (11010)_2 = (32)_8$$

$$5. (10110011)_2 = (?)_8$$

$$\begin{array}{|c|c|c|c|c|c|c|c|} \hline 1 & 0 & 1 & 1 & 0 & 0 & 1 & 1 \\ \hline \end{array}$$

2 6 3

$$\text{Ans:} - (10110011)_2 = (263)_8$$

$$6. (11011101)_2$$

$$\begin{array}{|c|c|c|c|c|c|c|c|} \hline 1 & 1 & 0 & 1 & 1 & 1 & 0 & 1 \\ \hline \end{array}$$

3 3 5

$$\text{Ans:} (11011101)_2 = (335)_8$$

Binary To Octal :-

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Fractional No :-

$$1. (11010110.1001)_2 = (?)_8$$

$$\begin{array}{ccccccc} 1 & 1 & 0 & 1 & 0 & 1 & 1 & 0 & . & 1 & 0 & 0 & 1 \\ \hline & 3 & & 2 & & 6 & & & & 1 & & & \end{array}$$

$$(11010110.1001)_2 = (326.44)_8$$

$$2. (11011101.10110)_2 = (?)_8$$

$$\begin{array}{ccccccc} 1 & 1 & 0 & 1 & 1 & 1 & 0 & 1 & . & 1 & 0 & 1 & 1 & 0 \\ \hline & 3 & & 3 & & 5 & & . & & 5 & & 4 & & \end{array}$$

$$(11011101.10110)_2 = (335.54)_8$$

2. Binary to Hexa :- (8421 Method).

$$1. (10110001100)_2 = (?)_{16}$$

$$\begin{array}{ccccccc} 1 & 0 & 1 & 1 & 0 & 0 & 0 & 1 & 1 & 0 & 0 \\ \hline & 8 & 4 & 2 & 1 & & 8 & 4 & 2 & 1 & & 8 & 4 & 2 & 1 \\ & 5 & & 8 & & & 12 & & & & & & & \end{array}$$

$$\text{Ans :- } (10110001100)_2 = (58C)_{16}$$

$$2. (1010101100)_2 = (?)_{16}$$

$$\begin{array}{r} 1010101100 \\ \hline 8421 \quad 8421 \quad 18421 \\ 2 \quad 10 \quad 12 \end{array}$$

$$\text{Ans: } (1010101100)_2 = (2AC)_{16}$$

\Rightarrow Fractional No :-

$$3. (\overline{11100101})_2, (\overline{11011})_2 = (?)_{16}$$

$$\begin{array}{r} 11100101.11011000 \\ \hline 8421 \quad 8421 \quad 8421 \quad 8421 \end{array}$$

$$\begin{array}{cccc} 14 & 5 & 13 & 8 \\ E & & BD & 8 \end{array}$$

$$\text{Ans: } (11100101.11011)_2 = (E5.B8)_{16}$$

9. Octal to Binary :-

$$1. (1234)_8 = (?)_2$$

$$\begin{array}{cccc} 1 & 2 & 3 & 4 \\ 001 & 010 & 011 & 100 \end{array}$$

$$\text{Ans: } (1234)_8 = (001010011100)_2$$

$$2. (2573)_8 = (?)_2$$

$$\begin{array}{cccc} 2 & 5 & 7 & 3 \\ 010 & 101 & 111 & 011 \end{array}$$

$$\text{Ans: } (2573)_8 = (010101111011)_2$$

⇒ Fractional No. \Rightarrow

$$1. (2614.435)_8 = (?)_2$$

$$\begin{array}{ccccccc} 2 & 6 & 1 & 4 & . & 4 & 3 & 5 \\ 010110 & 001100 & . & 100 & 011 & 101 & 101 \end{array}$$

$$\text{Ans: } (010110001100.00111010101)_2$$

10. Hexa to Binary \Rightarrow

$$1. (FA7)_{16} = (?)_2$$

$$\begin{array}{ccc} F & A & 7 \\ 1111 & 1010 & 0111 \end{array}$$

$$\text{Ans: } (FA7)_{16} = (111110100111)_2$$

$$2. (1AC)_{16} = (?)_2$$

$$\begin{array}{ccc} 1 & A & C \\ 0001 & 1010 & 1100 \end{array}$$

$$\text{Ans: } (1AC)_{16} = (000110101100)_2$$

$$8. (BCA)_{16} = (?)_2$$

| | | |
|------|------|------|
| B | C | A |
| 1011 | 1100 | 1010 |

$$\text{Ans: } (BCA)_{16} = (101111001010)_2$$

→ Fractional No^u

$$1. (2A2B.B4)$$

| | | | | | | |
|------|------|------|------|---|------|------|
| 2 | A | 2 | B | . | B | 4 |
| 0010 | 1010 | 0010 | 1011 | . | 1011 | 0100 |

$$\text{Ans: } (2A2B.B4) = (0010101000101011.10110100)$$

11. Hexa to Octal^u

→ 1. It is a two-step method.
 Step 1: Hexa to Binary
 Step 2: Binary to Octal.

$$1. (BCA)_{16} = (?)_8$$

$$\Rightarrow \text{Step 1: } (BCA)_{16} = (?)_2$$

| | | |
|---------------------|---------------------|---------------------|
| B ₍₁₀₁₁₎ | C ₍₁₁₀₀₎ | A ₍₁₀₁₀₎ |
| 1011 | 1100 | 1010 |

$$\Rightarrow (BCA)_{16} = (101111001010)_2$$

$$\text{Step 2: } (101111001010)_2 = (?)_8$$

$$101111001010$$

$$5107$$

$$\text{Ans: } (B(A)_{16} = (5712)_8$$

$$2. (A2DE)_{16} = (?)_8$$

Step 1: $(A2DE)_{16} = (?)_2$

$$(A2DE)_{16} = (?)_2$$

$$\begin{array}{cccc} A & 2 & D & E \\ (10) & & (13) & (14) \\ 1010001011011110 \end{array}$$

$$\rightarrow (A2DE)_{16} = (1010001011011110)_2$$

Step 2: $(1010001011011110)_2 = (?)_8$

$$(1010001011011110)_2 = (?)_8$$

$$\begin{array}{cccccc} 1010001011011110 \\ 1 \quad 2 \quad 1 \quad 3 \quad 3 \quad 6 \end{array}$$

$$\text{Ans: } (A2DE)_{16} = (121336)_8$$

$$3. (A37E)_{16} = (?)_8$$

$$A \quad 3 \quad 7 \quad E$$

$$\downarrow \quad \quad \downarrow$$

$$10 \quad 3 \quad 7 \quad 14$$

$$10 \quad 3 \quad 7 \quad 14$$

$$\text{Step 1: } (10 \quad 3 \quad 7 \quad 14)_{16} = (?)_2$$

$$101000110111110$$

$$(A37E)_{16} = (1010001101111110)_2$$

$$\text{Step 2: } (1010001101111110)_2 = (?)_8$$

$$1010001101111110$$

$$1 \quad 2 \quad 1 \quad 5 \quad 7 \quad 6$$

$$(A37E)_{16} = (121576)_8$$

$$4. (2BC4)_{16} = (?)_8$$

$$\begin{array}{cccc} 2 & B & C & 4 \\ & 11 & 12 & \end{array}$$

$$\text{Step 1: } \begin{array}{cccc} 2 & 11 & 12 & 4 \\ 0010 & 1011 & 1100 & 0100 \end{array} = (?)_8$$

$$\text{Step 2: } (0010101111000100)_2 = (?)_8$$

$$\begin{array}{cccccc} 0010 & 1011 & 1100 & 0100 \\ 2 & 5 & 7 & 0 & 4 \end{array}$$

$$(2BC4)_{16} = (25704)_8$$

⇒ Fractional No.

$$1. (D3.4C)_{16} = (?)_8$$

$$\text{Step 1: } \begin{array}{cc} D3 & . & 4C \\ \downarrow & & \downarrow \end{array}$$

$$\begin{array}{cc} 13 & 12 \end{array}$$

$$\begin{array}{cccc} 13 & 3 & 4 & 12 = (?)_8 \end{array}$$

$$\begin{array}{cccc} 1101 & 0011 & . & 0100 & 1100 \end{array}$$

$$\begin{array}{cccccc} 1101 & 0011 & . & 0100 & 1100 \\ 3 & 2 & 3 & 2 & 3 \end{array}$$

$$\text{Ans: } (D3.4C)_{16} = (323.23)_8$$

$$2. (1A.34)_{16} = (?)_8$$

1 A . 3 4

↓

10

$$\text{Step 1. } 1 \quad 10 \quad . \quad 3 \quad 00 \quad 4 \quad 111 = (?)_2$$

$$0001 \quad 1010 \quad . \quad 0011 \quad 0100$$

$$00011010 \cdot 00110100$$

$$0 \quad 3 \quad 2 \quad . \quad 1 \quad 5$$

$$\text{Ans: } (1A.34)_{16} = (032.15)_8$$

12. Octal to Hexa

$$1. (6357)_8 = (?)_{16}$$

$$\text{Step 1: } 6 \quad 3 \quad 5 \quad 7$$

$$110 \quad 011 \quad 101 \quad 111$$

$$110011101111$$

$$12 \quad 14 \quad 15$$

$$C \quad E \quad F$$

$$(6357)_8 = (CEF)_{16}$$

$$Q. (2761)_8 = (?)_{16}$$

$$\text{Step 1 :-} \quad \begin{array}{cccc} 2 & 7 & 6 & 1 \\ 010 & 111 & 110 & 001 \end{array}$$

$$\text{Step 2 :-} \quad \underline{01011110001}$$

$$5 \quad 15 \quad 1$$

F

$$(2761)_8 = (5F1)_{16}$$

→ Fractional No.

$$1. (1670.34)_8 = (?)_{16}$$

Step 1 :-

$$1670.34$$

$$001110111000.011100$$

Step 2 :-

$$\underline{001110111000.011100}$$

$$3 \quad 11 \quad 8 \quad 7 \quad 0$$

B

$$\text{Ans :-} (1670.34) = (3B8.70)_{16}$$

* Binary addition $_{2u} (1111) + _2 (0110011)$

Rules $_{2u}$

$$0 + 0 = 0$$

$$0 + 1 = 1$$

$$1 + 0 = 1$$

$$1 + 1 = 0 \text{ (carry 1)}$$

1. $(10001)_2 + (11101)_2$

$$\begin{array}{r} \\ \\ \\ + \\ \hline 1 0 1 1 0 \end{array}$$

Ans: $_{2u} (10001)_2 + (11101)_2 = (101110)_2$

2. $(100111)_2 + (11011)_2$

$$\begin{array}{r} \\ \\ \\ + \\ \hline 1 0 0 0 0 0 \end{array}$$

Ans: $_{2u} (100111)_2 + (11011)_2 = (1000010)_2$

3. $(1000111)_2 + (1011)_2$

$$\begin{array}{r} \\ \\ \\ + \\ \hline 1 0 1 0 0 0 \end{array}$$

$$A. (100111)_2 + (1111)_2$$

$$\begin{array}{r} 11 \\ 100111 \\ + 1111 \\ \hline 110110 \end{array}$$

→ Fractional No. :-

$$1. (1101.1)_2 + (1011.1)_2$$

$$\begin{array}{r} 111 \\ 1101.1 \\ + 1011.1 \\ \hline 11001.0 \end{array}$$

* Binary Subtraction :-

Rules :-

$$0 - 0 = 0$$

$$1 - 0 = 1$$

$$1 - 1 = 0$$

$$0 - 1 = 1 \text{ (Borrow 1)}$$

$$1. (10010)_2 \text{ from } (1011011)_2$$

$$\begin{array}{r} 1011011 \\ - 10010 \\ \hline 1001001 \end{array}$$

*. Multiplication No. 2

$$0 \times 0 = 0$$

$$0 \times 1 = 0$$

$$1 \times 0 = 0$$

$$1 \times 1 = 1$$

1. $(1111)_2$ by $(110)_2$

$$\begin{array}{r} 111 \\ \times 110 \\ \hline 11000 \\ 1110 \\ \hline 1111000 \\ \hline 101010 \end{array}$$

Ans: $(1111)_2 \times (110)_2 = (101010)_2$

2. $(00101001)_2$ by $(111)_2$

$$\begin{array}{r} 00101001 \\ \times 111 \\ \hline 0010001 \\ 00100010 \\ 001000100 \\ \hline 10001111 \end{array}$$

Ans: $(00101001)_2$ by $(111)_2 = (10001111)_2$

* Binary Division :- Rules.

$$0/1 = 0$$

$$1/1 = 0$$

1. $(10000111)_2$ by $(101)_2$

| | |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|
| $ \begin{array}{r} 101 \overline{) 10000111} \\ \underline{101} \\ 01000 \\ \underline{101} \\ 0100 \\ \underline{101} \\ 1 \end{array} $ | $ \begin{array}{r} 11011 \\ 101 \overline{) 10000111} \\ \underline{-101} \\ 0100 \\ \underline{-101} \\ 00111 \\ \underline{-101} \\ 0101 \\ \underline{-101} \\ 000 \end{array} $ |
|-----------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------------|

Ans: $(11011)_2$

2. $(101010)_2$ by $(110)_2$

$$\begin{array}{r}
 110 \overline{) 101010} \\
 \underline{-110} \\
 000 \\
 \underline{-110} \\
 0110 \\
 \underline{-110} \\
 000
 \end{array}$$

Ans: $(111)_2$

* Hexadecimal Arithmetic :-

→ Hexadecimal Addition :-

1. $(FACE)_{16} + (AB17)_{16}$

| | | | | | |
|---|-----------|----------|---------|----------|--|
| | 1 | 1 | | 1 | |
| | (15) | (10) | (12) | (14) | |
| | F | A | C | E | |
| + | (10) | (11) | 1 | 7 | |
| | A | B | 1 | 7 | |
| | 26 > 16 | 21 > 16 | 14 > 16 | 21 > 16 | |
| | -16 | -16 | E | -16 | |
| | <u>10</u> | <u>5</u> | | <u>5</u> | |
| | 10 | CA | | 5 | |

$$\begin{aligned} A &= 10 & D &= 13 \\ B &= 11 & E &= 14 \\ C &= 12 & F &= 15 \end{aligned}$$

Answer $(1A5E5)_{16}$

2. $(AC5A9)_{16} + (ED694)_{16}$

| | | | | | |
|---|----------|----------|---------|----------|---------|
| | 1 | 1 | | | |
| | (10) | (12) | | (10) | |
| | A | C | 5 | A | 9 |
| + | (14) | (13) | 6 | 9 | 4 |
| | E | D | 6 | 9 | 4 |
| | 25 > 16 | 25 > 16 | 11 > 16 | 19 > 16 | 13 > 16 |
| | -16 | -16 | C | -16 | D |
| | <u>9</u> | <u>9</u> | | <u>3</u> | |
| | 9 | 9 | | 3 | |

Answer $(199C3D)_{16}$

3. $(12.73)_{16} + (FD.B4)_{16}$

| | | | | | |
|-------------------|-------------------|-------------------|---|---|--|
| 1 | 1 | 1 | | | |
| 1 | 2 | 7 | 3 | | |
| F ₍₁₅₎ | D ₍₁₃₎ | B ₍₁₁₎ | 4 | + | |
| 17 | 16 | 18 | 7 | | |
| -16 | -16 | -16 | | | |
| 1 | 0 | 2 | | | |

Ans: $(110.27)_{16}$

→ Hexadecimal Subtraction :-

1. $(ABCD)_{16} - (56CF)_{16}$

| | | | | |
|-------------------|-------------------|-------------------|-------------------|--|
| | 16 | 16 | | |
| A ₍₁₀₎ | B ₍₁₁₎ | C ₍₁₂₎ | D ₍₁₃₎ | |
| - 5 | 6 | E ₍₁₄₎ | F ₍₁₅₎ | |
| 5 | 4 | 15 | 14 | |
| | | F | E | |

Ans: $(54FE)_{16}$

2. $(A27E9)_{16} - (6EB43)_{16}$

| | | | | | |
|-------------------|-------------------|-------------------|-------------------|----|---|
| | 9 | 16 | 16 | | |
| A ₍₁₀₎ | 2 | 7 | E ₍₁₄₎ | 9 | |
| - 6 | E ₍₁₄₎ | B ₍₁₁₎ | 4 | 3 | |
| 3 | 3 | 12 | C | 10 | 6 |

Ans: $(33CA6)_{16}$

$$3. (7E2CA)_{16} - (1F65)_{16}$$

$$\begin{array}{r}
 \begin{array}{cccc}
 & & 13 & 16 \\
 7 & E(14) & 2 & \\
 - & 1 & F(15) & 6 & 5 \\
 \hline
 7 & 12 & 3 & 6 & 5 \\
 & C & & &
 \end{array}
 \end{array}$$

$$\text{Answer } (7C865)_{16}$$

$$4. (52.33)_{16} - (4F.FF)_{16}$$

$$\begin{array}{r}
 \begin{array}{cccc}
 & & 16 & 16 & 16 \\
 54 & 2 & . & 32 & 3 \\
 - & 4 & F(15) & F(15) & F(15) \\
 \hline
 0 & 2 & . & 3 & 4
 \end{array}
 \end{array}$$

$$\text{Answer } (52.33)_{16} - (4F.FF)_{16} = (2.34)_{16}$$

* Octal Arithmetic

1. $(1670)_8 + (1256)_8$

$$\begin{array}{r}
 1 1 \\
 1 6 7 0 \\
 + 1 2 5 6 \\
 \hline
 3 9 2 8 12 8 6 7 8
 \end{array}$$

$$\begin{array}{r}
 3 9 12 6 \\
 -8 -8 \\
 \hline
 3 1 4 6
 \end{array}$$

Ans $(1670)_8 + (1256)_8 = (3146)_8$

2. $(5647)_8 + (1425)_8$

$$\begin{array}{r}
 1 1 \\
 5 6 4 7 \\
 + 1 4 2 5 \\
 \hline
 7 7 8 10 7 8 7 7 8 12 7 8
 \end{array}$$

$$7 (10-8)2 7 (12-8)=4$$

Ans: $(5647)_8 + (1425)_8 = (7274)_8$

 \Rightarrow Subtraction :-

1. $(745)_8 - (574)_8$

$$\begin{array}{r}
 6 8 \\
 7 4 5 \\
 - 5 7 4 \\
 \hline
 1 5 1
 \end{array}$$

$= (151)_8$

* Complementary Method :-

1. Find the complement of $(37)_{10}$

→ Here, the number has two digits and the value of Base is 10. Now formula is $(\text{Base})^n - 1$.

$$\therefore (10)^2 - 1$$

$$\therefore 100 - 1$$

$$\therefore 99$$

$$\text{Now, } 99 - 37 = 62.$$

Ans:- Complement of $(37)_{10} = (62)_{10}$.

2. $(56)_{10}$

$$\rightarrow n = 2.$$

$$(\text{Base})^n - 1$$

$$(10)^2 - 1$$

$$100 - 1$$

$$99$$

$$\text{Now, } 99 - 56 = 43$$

Ans:- Complement of $(56)_{10} = (43)_{10}$

3. $(35)_{10}$

$$n = 2.$$

$$(\text{Base})^n - 1$$

$$(10)^2 - 1$$

$$100 - 1 = 99.$$

$$\text{Now, } 99 - 35 = 64$$

Ans:- Complement of $(35)_{10} = (64)_{10}$

$$4. (53)_{10}$$

$$n = 2$$

$$(Base)^n - 1$$

$$(10)^2 - 1$$

$$100 - 1$$

$$99$$

$$\text{Now, } 99 - 53 = 46$$

Ans:- Complement of $(53)_{10} = (46)_{10}$

* 2. Complement method for subtraction

Rules for complement :-

$$1. 1's = 0$$

$$2. 0's = 1$$

→ 1. Subtracting smaller no. from a bigger one.

$$1. (10010)_2 - (01001)_2$$

Step 1 Convert $(01001)_2$ into 1's complement
i.e. $(01001)_2$ complement is $(10110)_2$

Step 2 :- Add this no. into $(10010)_2$

$$\begin{array}{r} 10010 \\ + 10110 \\ \hline \end{array}$$

$$\begin{array}{r} 10010 \\ + 10110 \\ \hline 101000 \end{array}$$

$$101000$$

Step 3:- When subtract smaller number from a bigger number and by adding the second no, you must get a carry which is dropped and incremented by 1.

$$\begin{array}{r} 01000 \\ + \quad \quad \quad 1 \\ \hline 1001 \end{array}$$

Ans:- $(1001)_2$.

* 2. Subtracting bigger no. from smaller one
 $(1001)_2 - (10011)_2$.

Step 1 :- Convert $(10011)_2$ into 1's complement i.e. $(10011)_2$ is $(01100)_2$.

Step 2 :- Add this no. into $(1001)_2$

$$\begin{array}{r} 01001 \\ + 01100 \\ \hline 10101 \end{array}$$

Step 3 :- When subtract a bigger no. from smaller no. and by adding complement into second number, you always get a result without a carry.

Now again complement the result and

add - sign.

Complement of result.
 $10101 = 01010$

Ans :- $(01010)_2$

3. $(110101)_2 - (111011)_2$

Step 1:- Convert $(111011)_2$ into 1's complement
 i.e. $(111011)_2$ complement is $(000100)_2$

Step 2:- Add this no. into $(110101)_2$

$$\begin{array}{r}
 110101 \\
 + 000100 \\
 \hline
 111001
 \end{array}$$

Step 3:- When subtract a bigger no. from smaller no. and by adding complement into second no., you always get a result without a carry. add - sign.

Complement of result:-
 $(111001)_2 = (000110)_2$

Ans:- $(000110)_2$

$$4. (10011)_2 - (10010)_2$$

Step 1 :- Convert $(10010)_2$ into its complement
 i.e. $(10010)_2 = (01101)_2$

Step 2 :- Add $(10011)_2$ to $(01101)_2$

$$\begin{array}{r} 1111 \\ 10011 \\ + 01101 \\ \hline 00000 \end{array}$$

Step 3 :- Add $(00000)_2$ increment by 1

$$\begin{array}{r} 00000 \\ + 1 \\ \hline 00001 \end{array}$$

$$\text{Ans :- } (00001)_2 \rightarrow (1)_2$$

* Parity Scheme :-

During a transmission of data there is a possibility of errors due to disturbance.

→ Most of this error result in change of 0 to 1 or 1 to 0.

→ For detecting the error parity bit is attached.

① → A parity bit is an extra bit which

is added in the binary data such that it makes the total number of 1 either even or odd.

→ Parity scheme for even parity is 1 and for odd parity is 0.

* Character Code :-

→ Code is a symbolic representation of different information which may be represented in form of numbers, letters or physical quantities.

1. BCD :-

Binary Coded Decimal.

→ In BCD number system each decimal digit is represented by a binary code of 4 digit.

→ Binary weight of the 4 bit is $2^0, 2^1, 2^2, 2^3$

2. EBCDIC :-

Extended Binary coded of Decimal information Code.

→ It was 8 bits for each character.

→ It was divided into two, 4 bit group.

3. ASCII :- American Standard Code of Information Interchange.

4. UNICODE :-

→ This code is popular in data communication and use to represent data in micro computer.

Questions :-

- Q1. What is serial ports and parallel ports
- Q2. What is port explain USB port in detail. [2]
- Q3. What is BIOS [2]
- Q4. Define POST [2]
- Q5. Define a block diagram of computer and explain all its function unit [5]
- Q6. Number System [16][18]
- Q7. What is EBCDIC [2]
- Q8. What is ASCII [2]
- Q9. What is Parity Scheme [2]
- Q10. Explain Motherboard in detail [5]
- Q11. Explain different phases of Machine cycle [5]
- Q12. Define term BUS and PORT [2]
- Q13. What is Databus & Address bus [2]
- Q14. Functionality of Input unit [2]
- Q15. Why computer is also known as dataprocessor [2]